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VIBRATION AND KINEMATIC ANALYSIS OF SCARA ROBOT STRUCTURE

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ABSTRACT:-This paper presents a procedure for assessing the vibration analysis of type SCARA robots. The motion and running conditions of such robots are very complicated that leads to produce vibration and shock which are generated by arm profile in running conditions. In this study the vibration analysis gives the feasibility of the preview control was examined to improve the performance of the SCARA robots system. As it is important for containment the robot arm trajectories generated by the model to show satisfactory safe performance under vibration occurrence phenomena so that they completely avoid errors, the results obtained from such vibration analysis assessment procedure are considered to be valuable and reliable process not only with respect to vibration risk assessment but also for predicting kinematic analysis by investigating the robot arm motion using the kinematic and vibration methods. Forced vibrations is studied analytically help the designer to predict the behavior and design the robot hardware or control system. Theoretical results show reduction in both vibration amplitude and time history response.

Keywords:-SCARA robot, vibration analysis, Modeling, Control Kinematic analysis.

1- INTRODUCTION

SCARA robot is one of the industrial robots which can replace humans in carrying out various types of operations. They can as well serve machine tools as to carry out various tasks like welding, handling, painting, assembling, automotive, electronics and other industries. SCARA robots have two rotational joints on a horizontal plane and usually one translational joint on the vertical axis. The structure of SCARA robots is simple and they are widely used all over the world because the structure is suitable for automation lines and other

industrial purposes. SCARA robots are in particular utilized for pick-and-place task. In such cases, the motion of SCARA robots commonly is periodic.

The robot was developed in the laboratory of Professor Makino at Japan's Yamanashi University (Makino and Furuya)⁽¹⁾. Various studies were devoted to this architecture. A dynamic modeling and linearization technique for a SCARA robot was presented by Tern et al. ⁽²⁾. A new energy-saving method for SCARA robots was proposed by Guangqiang Lu et.al. (3). To effectively reduce energy consumption, nonlinear robot dynamics are mechanically liberalized in this paper. A complete mathematical model of SCARA robot including servo actuators dynamics with dynamic simulation was presented by Mahdi et. al ⁽⁴⁾. A simple method for estimating the dynamic parameters of SCARA robot has been presented by Yan Meng and S.P.Chen⁽⁵⁾. Residual vibrations of industrial SCARA robots in wafer handling applications were investigated by WeiMIN et. al. ⁽⁶⁾. Philip Voglewede et. at. ⁽⁷⁾ were studied the dynamic performance of a SCARA robot manipulator with uncertainty using polynomial chaos theory. Dynamic calibration of SCARA robot was presented by M. Indri et. al.⁽⁸⁾. Mathematical modeling, simulation and experimental verification of a SCARA robot were presented by Das, M.T. and L. C. Dulger⁽⁹⁾. Appropriate Mathematical Model of DC Servo Motors Applied in SCARA Robots was presented by Attila L. Bencsik⁽¹⁰⁾. A mathematical model for an industrial track robot was proposed by WeiMIN Tao et. al. ⁽¹¹⁾. A complete mathematical model of SCARA robot and the PD controller for each robot joint is presented by Das T. and Dülger C.⁽¹²⁾.

The Selective Compliant Articulated/Assembly Robot Arm (SCARA) as shown in figure (1) is usually a 4-axis industrial robot. The kinematics is like a human arm, with the first joint being referred to as the shoulder and the second as the elbow. These two joints allow movement in the X- and Y- axes. The third joint is a translation joint and moves along the Z-axis. The last joint, called Theta-Z, gives a rotation around the Z-axis (wrist rotation).

The first robot arm articulated on the robot console and swivel able about a first swivel axis as shown in figure (2), and second swivel arm articulated on the first swivel arm and swivel able around the second swivel axis extending substantially parallel to the first swivel axis, at least one work unit, at least one first swivel motor for swiveling an arm unit composed of the first and second robot arms relative to the robot console, at least one second swivel motor for turning the second robot arm relative to the first robot arm, and at least one work motor for actuating the work unit, with the motors being controllable by a power electronics, with electrical circuits including convertor circuits for current supply of the motors and at least one control circuit for operating the convertor circuits and thereby for controlling the motors, and with at least one rectifier circuit being received in at least one robot arm.

Vibration and kinematic analysis of SCARA robot are presented in this paper. In a kinematic analysis the position, velocity and acceleration of all links are calculated without considering the forces that cause this motion. The relationship between motion, and the associated forces and torques is studied in robot dynamics ⁽¹³⁾. The kinematic separate in two types, direct kinematics and inverse kinematics. In forward kinematics, the length of each link and the angle of each joint is given and we have to calculate the position of any point in the work volume of the robot. In inverse kinematics, the length of each link and position of the point in the work volume is given and we have to calculate the angle of each joint. Vibration analysis of this model using Lagrange's approach was made to obtain frequency equation the dynamic stiffness method applies mainly to excitations of harmonic nodal forces. For vibrational loading, modal analysis is generally required. This study analyzes the effects of vibration loading on the dynamic stability of a force-controlled flexible manipulator. The forced vibration analysis is then carried out to obtain the eigenvalues and eigenvectors. The modal approach for applied loading leads to the formulation of a model used to predict the behavior of the SCARA robot. The aim of using MATLAB-Simulink-Sim Mechanics is to build the model and to analyze the kinematic equation. The results of kinematic and vibration analysis using MATLAB/Simulink software are presented.

2- KINEMATIC ANALYSIS:

The mathematical model of a two-joint type SCARA robot is illustrated ⁽¹⁵⁾. For the mass centers of the robot links are concentrated at the centers of the arm. Hence, the two l inks have the same moments of inertia. Table (1) shows the parameters of the two-link rigid - type robot. The geometry of SCARA robot is shown in Fig (3).

The positions, velocities, and acceleration of SCARA robot shown in Fig. (3), can be obtained by using the kinematic analysis and the aid of the Euler' identity as ⁽¹⁶⁾:

$$\theta_1 = 2 \tan^{-1} \left(\frac{-Q \pm \sqrt{(Q^2 - 4*P*R)}}{2*P} \right)$$
(1)

$$\theta_2 = 2 \tan^{-1} \left(\frac{-T \pm \sqrt{(T^2 - 4 * S * U)}}{2 * S} \right) \tag{2}$$

Where

$$P = \frac{a^2 - b^2 + c^2 + d^2}{2a} + d, \quad Q = -2c \text{, and } R = \frac{a^2 - b^2 + c^2 + d^2}{2a} - d \tag{3}$$
$$S = \frac{a^2 - b^2 - c^2 - d^2}{2b} + d, T = -2c \text{, and } \quad U = \frac{a^2 - b^2 - c^2 - d^2}{2b} - d \tag{4}$$

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The angular velocities of SCARA robot links are given by:

$$\omega_1 = \frac{\dot{c} \tan \theta_2 + \dot{d}}{a \left(\cos \theta_1 \tan \theta_2 - \sin \theta_1\right)}$$
(5)
$$\omega_2 = \frac{\dot{c} \tan \theta_1 + \dot{d}}{1 \left(\cos \theta_1 \sin \theta_2 - \sin \theta_1\right)}$$
(6)

$$\omega_2 = \frac{c \tan \theta_1 + u}{b \left(\cos \theta_2 \tan \theta_1 - \sin \theta_2\right)} \tag{6}$$

And the angular acceleration are:

$$\alpha_1 = \frac{a\omega_1^2 \sin \theta_1 - (a\omega_1^2 \cos \theta_1 \cot \theta_2 + b\omega_2^2 \cos \theta_2 \cot \theta_2 + \ddot{d} \cot \theta_2) + \ddot{c} + b\omega_2^2 \sin \theta_2}{a(\cos \theta_1 + \sin \theta_1 \cot \theta_2)}$$
(7)

$$\alpha_2 = \frac{a\alpha_1 \sin\theta_1 + a\omega_1^2 \cos\theta_1 + b\omega_2^2 \cos\theta_2 + \ddot{a}}{b\sin\theta_2} \tag{8}$$

The translation accelerations of the links are:

$$A_1 = aj\alpha_1 e^{j\theta_1} - a\omega_1^2 e^{j\theta_1} \tag{9}$$

$$A_2 = bj\alpha_2 e^{j\theta_2} - b\omega_2^2 e^{j\theta_2} \tag{10}$$

$$A_3 = \ddot{c} \tag{11}$$

$$A_4 = \ddot{d} \tag{12}$$

3- VIBRATION ANALYSIS

The uncoupled equations of motion of a SCARA robot (as modeled in figure (4)), subjected to vibrational loading can be derived by menus of the Lagrange's equation approach as:

The kinetic energy of the robot can be written as:

$$\mathbf{K} \cdot \mathbf{E} = \frac{1}{2} \mathbf{m}_{1} \left(\frac{1}{2} \mathbf{L}_{1} \dot{\mathbf{\theta}}_{1} \right)^{2} + \frac{1}{2} \mathbf{m}_{1} \left(\mathbf{L}_{1} \dot{\mathbf{\theta}}_{1} \right)^{2} + \frac{1}{2} \mathbf{m}_{2} \mathbf{v}_{2}^{2} + \frac{1}{2} \mathbf{m}_{2} \left(\mathbf{L}_{2} \dot{\mathbf{\theta}}_{2} \right)^{2}$$
(13)

Where, for small angle

$$v_2^2 = \left(L_1 \dot{\theta}_1 + \frac{1}{2} L_2 \dot{\theta}_2\right)^2 \tag{14}$$

By substituting equation (14) in equation (13) & rearranging yields;

$$\mathbf{K} \cdot \mathbf{E} = \frac{1}{2} \mathbf{m}_{1} \left(\frac{1}{2} \mathbf{L}_{1} \dot{\boldsymbol{\theta}}_{1} \right)^{2} + \frac{1}{2} \mathbf{m}_{1} \left(\mathbf{L}_{1} \dot{\boldsymbol{\theta}}_{1} \right)^{2} + \frac{1}{2} \mathbf{m}_{2} \left(\mathbf{L}_{1} \dot{\boldsymbol{\theta}}_{1} + \frac{1}{2} \mathbf{L}_{2} \dot{\boldsymbol{\theta}}_{2} \right)^{2} + \frac{1}{2} \mathbf{m}_{2} \left(\mathbf{L}_{2} \dot{\boldsymbol{\theta}}_{2} \right)^{2}$$
(15)

The potential energy of the SCARA robot can be written as:

$$P.E = \frac{1}{2}m_{1}gL_{1}(1 - \cos\theta_{1}) + m_{2}g\left(L_{1}(1 - \cos\theta_{1}) + \frac{1}{2}L_{2}(1 - \cos\theta_{2})\right)$$
(16)

After differentiating the equation (15) first for $\dot{\theta}_1$ and then with respect to time we obtain:

$$\frac{\mathrm{d}}{\mathrm{dt}}\left(\frac{\partial \mathrm{K.E}}{\partial \dot{\theta}_{1}}\right) = \left(\frac{5}{4}\mathrm{m}_{1} + \mathrm{m}_{2}\right)\mathrm{L}_{1}^{2}\ddot{\theta}_{1} + \frac{1}{2}\mathrm{m}_{2}\mathrm{L}_{1}\mathrm{L}_{2}\ddot{\theta}_{2}$$
(17)

Differentiating the equation (16) with respect to θ_1

$$\frac{\partial \mathbf{P}.\mathbf{E}}{\partial \theta_{1}} = \frac{1}{2} \mathbf{m}_{1} \mathbf{g} \mathbf{L}_{1} \sin \theta_{1} + \mathbf{m}_{2} \mathbf{g} \mathbf{L}_{1} \sin \theta_{1}$$
(18)

And, for a small angle

$$\therefore \frac{\partial P.E}{\partial \theta_{1}} = \left(\frac{1}{2}m_{1} + m_{2}\right)gL_{1}\theta_{1}$$

$$\frac{\partial K.E}{\partial \theta_{1}} = 0 \qquad ; \frac{\partial D.E}{\partial \dot{\theta}_{1}} = 0 \qquad ; Q_{1} = 0$$
(19)
(20)

After repeating the same procedure for kinetic and potential energies for θ_2 , we obtained

$$\frac{\mathrm{d}}{\mathrm{dt}}\left(\frac{\partial \mathrm{K.E}}{\partial \dot{\theta}_{2}}\right) = \frac{1}{2}m_{2}L_{1}L_{2}\ddot{\theta}_{1} + \frac{5}{4}m_{2}L_{2}^{2}\ddot{\theta}_{2}$$
(21)

$$\frac{\partial \mathbf{P}.\mathbf{E}}{\partial \theta_2} = \frac{1}{2} \mathbf{m}_2 \mathbf{g} \mathbf{L}_2 \theta_2$$
(22)

$$\frac{\partial K.E}{\partial \theta_2} = 0 \qquad \qquad ; \frac{\partial D.E}{\partial \dot{\theta}_2} = 0 \qquad \qquad ; Q_2 = F_{\circ}$$
(23)

Lagrange's equation approach is:

$$\frac{d}{dt}\left(\frac{\partial K.E}{\partial \dot{q}_{i}}\right) - \frac{\partial K.E}{\partial q_{i}} + \frac{\partial P.E}{\partial q_{i}} + \frac{\partial D.E}{\partial \dot{q}_{i}} = Q_{i}$$
(24)

By substituting the equations (17, 19, and 20) in Lagrange's equation yields

$$\left(\frac{5}{4}m_{1}+m_{2}\right)L_{1}^{2}\ddot{\theta}_{1}+\frac{1}{2}m_{2}L_{1}L_{2}\ddot{\theta}+\left(\frac{1}{2}m_{1}+m_{2}\right)gL_{1}\theta_{1}=0$$
(25)

And. by substituting the equations (21, 22, and 23) in Lagrange's equation we obtain:

$$\frac{1}{2}m_2L_1L_2\ddot{\theta}_1 + \frac{5}{4}m_2L_2^2\ddot{\theta}_2 + \frac{1}{2}m_2gL_2\theta_2 = F_{\circ}$$
⁽²⁶⁾

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Now writing the equation of motion (25, 26) of the SCARA robot in matrix form:

$$\begin{bmatrix} \left(\frac{5}{4}\boldsymbol{m}_{1}+\boldsymbol{m}_{2}\right)\mathbf{L}_{1}^{2} & \frac{1}{2}\boldsymbol{m}_{2}\mathbf{L}_{1}\mathbf{L}_{2} \\ \frac{m_{2}}{2}\mathbf{L}_{1}\mathbf{L}_{2} & \frac{5}{4}\boldsymbol{m}_{2}\mathbf{L}_{1}^{2} \end{bmatrix} \begin{bmatrix} \ddot{\boldsymbol{\theta}}_{1} \\ \ddot{\boldsymbol{\theta}}_{2} \end{bmatrix} + \begin{bmatrix} \left(\frac{m_{1}}{2}+\boldsymbol{m}_{2}\right)\mathbf{g}\mathbf{L}_{1} & \mathbf{0} \\ \mathbf{0} & \frac{m_{2}}{2}\mathbf{g}\mathbf{L}_{2} \end{bmatrix} \begin{bmatrix} \boldsymbol{\theta}_{1} \\ \boldsymbol{\theta}_{2} \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{F}_{0} \end{bmatrix}$$
(27)

4- EIGEN VALUES & EIGEN VECTORS

Using the dynamic matrix procedure to determine the eigenvalues (natural frequencies) and eigenvectors (mode shapes) of the SCARA robot as:

$$[\mathbf{M}]\{\ddot{\boldsymbol{\theta}}\} + [\mathbf{K}]\{\boldsymbol{\theta}\} = 0$$
⁽²⁸⁾

Eigenvalues (natural frequencies)

$$\therefore |[\mathbf{D}] - \lambda [\mathbf{I}]| = 0 \tag{29}$$

Eigenvectors (mode shapes):

$$[[D] - \lambda [I]] \phi_{ij} = 0$$
⁽³⁰⁾

Time response:

$$\begin{cases} \theta_1 \\ \theta_2 \\ \end{cases} = \begin{cases} A_1 \\ A_2 \\ \end{cases} \sin(\omega t + \psi) \implies \begin{cases} \ddot{\theta}_1 \\ \ddot{\theta}_2 \\ \end{cases} = -\omega^2 \begin{cases} A_1 \\ A_2 \\ \end{cases} \sin(\omega t + \psi) \qquad (31)$$
$$\begin{cases} f_0 \\ 0 \\ \end{cases} = \begin{cases} f_0 \\ 0 \\ \end{cases} \sin(\omega t + \psi)$$

For generalized response for SCARA robot is:

$$q_{i}(t) = \sum_{j=1}^{n} A_{j} \phi_{ij} \sin\left(\omega_{j} t + \psi_{j}\right)$$
(32)

$$q_{1}(t) = A_{1}\phi_{11}\sin(\omega_{1}t + \psi_{1}) + A_{2}\phi_{12}\sin(\omega_{2}t + \psi_{2})$$
(33)

$$q_{2}(t) = A_{1}\phi_{21}\sin(\omega_{1}t + \psi_{1}) + A_{2}\phi_{22}\sin(\omega_{2}t + \psi_{2})$$
(34)

The phase angles (Ψ) can be determined from the four initial conditions of the SCARA robot:

Initial displacement:

$$q_1(0) = 0$$
 , $q_2(0) = 0$ (35)

Initial velocities:

$\dot{q}_1(\mathbf{0}) = \mathbf{0}$, $\dot{q}_2(\mathbf{0}) = \mathbf{0}$ (36)

By substituting the four initial conditions in equation's (42, 43), we can obtained the phase angle.

5- RESULTS ANDDISCUSSION

The end effector coordinates of the robotic arm (x and y) are located by using the forward kinematics and meshgrid command in MATLAB package by introducing the values of the positions θ_1 and θ_2 when the ranges of the angles θ_1 and θ_2 are $0 \le \theta_1 \le 180^\circ$ and $0 \le \theta_2 \le 180^\circ$ respectively, as shown in Fig. (5).

In fig. (6),we can see the X-Y coordinates are generated for all θ_1 and θ_2 combination by using the forward kinematics for $0 \le \theta_1 \le 360^\circ$ and $0 \le \theta_2 \le 360^\circ$.

When using inverse kinematics analysis by introducing the above values of (x and y) to MATLAB program of the derived equations (1and 2), to get the same value of angles relative to forward kinematics as shown in figure (7). By using MATLAB-Simulink-Sim Mechanics to build the model and to analyze the kinematic equations, the same results for position, velocity, and acceleration of the SCARA robot were found comparison to the results which obtained when using derived equations, as shown in Figs. (9-11).

The frequency response of the SCARA robot is computed for a range of values of exciting frequencies. The exciting load is a constant force Fo applied at the free end for the second link as shown in Fig. (12).

6- CONCLUSION

Vibration and kinematics analysis of SCARA robot are presented in this paper. Also, the Simulation studies were performed by using MATLAB software. The main concluding remarks of the paper can be summarized as follows:

1- The model analysis of SCARA robot was performed. The natural frequencies and mode shapes were obtained for several parameters combination. Frequency response analysis was performed by finding the vibrational amplitudes and the accumulated deflections in the free end of the robot.

- 2- Dynamic analysis to analyze SCARA robot subject to loads that vary with time or frequency where all links of the robot have resonant or natural frequencies, and if the structure is excited at, or close to one of these frequencies then a very high amplitude response can occur. Therefore, it is necessary to ensure in the design of the SCARA robot that the resonant and excitation frequencies are not close to each other.
- 3- The behavior of a structure to time-varying excitation is computed. Frequency response analysis computes the structural response to steady-state oscillatory excitation. In addition, it is also possible to conduct a random analysis with frequency response.
- 4- MATLAB/ Simulink, structure for SCARA robot are built which enables the researchers to investigate the robot parameters using both forward and inverse kinematics.
- 5- An agreement between the results for derived equation and the MATLAB software is certainly obtained herein.

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NOMENCLATURE:

[K]	Stiffness	matrix,	[N/m]	
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[M]	Mass	matrix.	[kg]
	111400		1

- [D] Dynamical Matrix
- [I] Identity Matrix
- Q₁, Q₂ External Force [N]
- L_i Robot link length, [mm], (i =1, 2)
- *m*1, *m*2 masses of Robot links1 and 2 respectively [kg]
- g Gravity [m/s²]
- F_o Excitation force [N]

а

- ω_1 , ω_2 Angular velocities of links1 and 2 respectively (rad/sec).
- A_3 , A_4 Translation accelerations of links 3 and 4 respectively (m/sec²).
- \dot{c} , \dot{d} Linear velocities of links3 and 4 respectively (m/sec).
- α_1 , α_2 Angular accelerations of links 1 and 2 respectively (rad/sec²).
 - Length of link 1 (m).
- b Length of link 2 (m).
- c Length of link 3 (it represents y component of robot's tip) (m).
- d Length of link 4 (it represents x component of robot's tip) (m).
- θ_i Angle of links (degree), (i = 1,2,3,4).

 Table (1): Parameters of the two-link rigid -type robot.

Link	Mass(kg)	Length (m)	Tensor of Moment of inertia(kg*m ²)	
			[x y z]	
1	1	1	[0.083 0 0;0 0 0; 0 0 0.083]	
2	1	1	[0.083 0 0;0 0 0; 0 0 0.083]	













Figure (6): X-Y generated for all θ_1 and θ_2 combinations using forward kinematics (where $0 \le \theta_1 \le 360^\circ$ and $0 \le \theta_2 \le 360^\circ$



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Figure (9): Theta2 versus Theta1 for derived equations and Simulink model.

Figure (10): Angular velocities by derived equations and Simulink model.

Figure (11): Angular acceleration by derived equations and Simulink model.

Figure (12): Mode shape of SCARA robot.

التحليل الاهتزازي والحركي لهيكل الروبوت SCARA

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الخلاصة

يعرض هذا البحث إجراء تحليل لتقييم اهتزاز الروبوتات نوع SCARA. شروط الحركة والتشغيل لمثل هذا النوع من الروبوتات معقدة جدا بحيث تودي إلى نشوء اهتزازات وصدمة متولدة عن مسار ذراع الروبوت خلال ظروف التشغيل.وفي هذه الدراسة يعطي تحليل الاهتزازات جدوى السيطرة المعاينة لتحسين أداء نظام الروبوتات SCARA كما أنه من المهم احتواء مسارات ذراع الروبوت التي تم إنشاؤها بواسطة نموذج لإظهار أداء مقبولا وآمنا تحت ظاهرة حدوث الاهتزاز لتجنب الأخطاء تماما. أن هذه النتائج التي تم المحصول عليها من خلال إجراء تحليل لتقييم الاهتزاز يمكن اعتبارها ذات قيمة عملية وموثوقة، ليس فقط فيما يتعلق تقييم مخاطر الاهتزاز ولكن أيضا للتنبؤ بالتحليل الكينيماتيكي من خلال تخمين حركة اذرع الروبوت باستخدام الطرق الكينيماتيكية والاهتزاز .تم دراسة الاهتزازات القسرية تحليليا لمساعدة المصممين للتنبؤ بسلوك وتصميم أجهزة الروبوت أو نظام التحكم .النتائج النظرية بينت انخفاضا في سعة الاهتزاز ومسار الاستجابة